

Cosmonaut Vassily encounters an alien artifact in space: a big hoop of radius $R = 7.7 \text{ m}$ mass $M = 596 \text{ kg}$

The object spins slowly at $\omega = 0.17 \frac{\text{rad}}{\text{s}}$.

The moment of inertia is

$$I = MR^2 = (596 \text{ kg})(7.7 \text{ m})^2 = 35,337 \text{ kg}\cdot\text{m}^2$$

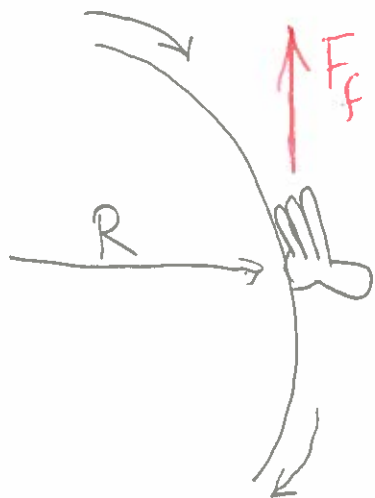
The kinetic energy of rotation is

$$\begin{aligned} KE &= \frac{1}{2} I \omega^2 = \frac{1}{2} (35,337 \text{ kg}\cdot\text{m}^2) \left(0.17 \frac{\text{rad}}{\text{s}}\right)^2 \\ &= 511 \text{ J} \end{aligned}$$

Vassily presses his glove against the hoop, exerting a normal force $F_N = 48 \text{ N}$, with coeff of kinetic friction $\mu_k = 0.25$.

The friction force on the hoop is

$$F_f = F_N \cdot \mu_k = 12 \text{ N}$$



The torque around the center of the hoop due to this force is

$$\begin{aligned} \tau &= |R| |F_f| \sin 90^\circ \\ &= 92.4 \text{ N}\cdot\text{m} \quad \text{out of page} \end{aligned}$$

Due to this torque, the hoop's angular velocity starts to change. The magnitude of the angular acceleration is

$$|\alpha| = \frac{|\tau|}{I} = \frac{92.4 \text{ N}\cdot\text{m}}{35,337 \text{ kg}\cdot\text{m}^2} = 0.00262 \frac{\text{rad}}{\text{s}^2}$$

If Vassily continues to exert this torque, the wheel will eventually come to a halt.

$$\omega_f = \omega_i + \alpha t$$

$$0 \frac{\text{rad}}{\text{s}} = 0.17 \frac{\text{rad}}{\text{s}} + \left(-0.00262 \frac{\text{rad}}{\text{s}^2}\right) t$$

$$\Rightarrow t = \frac{-0.17 \frac{\text{rad}}{\text{s}}}{0.00262 \frac{\text{rad}}{\text{s}^2}} = \underline{\underline{65.0 \text{ s}}}$$